

Order of Magnitude

The order of magnitude of a number is the number expressed to the nearest ^{integer} whole number power of 10.

Pop of Earth: 6.9 billion 6.9×10^9

between 10^9 and 10^{10}

order of magnitude is 10^{10}

Gravitational field strength 9.8 N kg^{-1}

b/w 10^0 and 10^1

order of magnitude is 10^1 or 10

Mass of an electron: $9.1 \times 10^{-31} \text{ kg}$

b/w 10^{-31} and 10^{-30}

order of magnitude is 10^{-30}

Try these:

1. Atmospheric Pressure at sea level $1.01 \times 10^5 \text{ Pa}$ 10^5
2. Average height of a adult mal 1.784 m 10^0 m
3. Box of apples has a mass of 16 kg 10
4. Cheese 0.075 kg 10^{-1} kg

Rounding with orders of magnitude:

cut off 3.16

Try these:

4.13×10^3

~~10^3~~ 10^4 ✓

3.09×10^{-6}

10^{-6} ~~10^{-5}~~

4245

10^3 10^4

$3.3 > 3.16$

0.00033

10^{-4} 10^{-3}

3.3×10^{-4}

Example:

Which of the following is the same as 3.8×10^{-3} to the nearest order of magnitude? 10^{-3} and 10^{-2}

~~a)~~ 3.0×10^{-3}

~~b)~~ 4.0×10^{-2}

c) 10^{-2}

d) 10^{-3}

$3.8 > 3.16$

round up the order of magnitude.

Very Large numbers / Very small numbers

We are limited by what we can visualize or we have experienced.

objects in this room $\sim 1\text{ m}$

strand of hair $\sim 0.1\text{ mm}$ or 10^{-4} m

distance to moon $\sim 10^9\text{ m}$

Can you visualize the speed of light?

$$c = 3.0 \times 10^8 \text{ m s}^{-1}$$

- light would travel back + forth across this room a million times every second (about).
- light takes 8 minutes to reach the Earth from the Sun.
- LHC (Large Hadron Collider)
 - 27 km long
 - protons travel at almost the speed of light.
 - travel around the collider 10,000 times a second.
- it takes light 4 years to get to the Earth from our nearest star and 100,000 years to cross Milky way.

You MUST KNOW these:

Distances:

Diameter of a proton 10^{-15} m

Extent of the visible universe 10^{25} m

Masses:

Mass of the electron 10^{-30} kg

Mass of the universe 10^{50} kg

Times:

Time for light to cross a nucleus 10^{-23} s

Age of universe 10^{18} s

Ratios are expressed as a difference in orders of magnitude:

Compare

$$\frac{\text{diameter of H atom}}{\text{diameter of H nucleus}} = \frac{10^{-10}}{10^{-15}} = 10^5$$

The diameter of the H atom is 10^5 orders of magnitude larger than the diameter of the nucleus

Example:

The diameter of a proton is about 10^{-15} m and the diameter of a hydrogen atom is about 10^{-10} m.

just a proton for hydrogen

How many orders of magnitude is the volume of a hydrogen atom greater than the volume of its nucleus?

$$V = \frac{4}{3}\pi r^3$$

$$\frac{\text{volume of H atom}}{\text{volume of nucleus}} = \frac{\frac{4}{3}\pi \left(\frac{d_{\text{atom}}}{2}\right)^3}{\frac{4}{3}\pi \left(\frac{d_{\text{nuc}}}{2}\right)^3}$$

$$= \frac{d_{\text{atom}}^3}{d_{\text{nuc}}^3}$$

The volume of the hydrogen atom is 10^{15} times bigger than its nucleus (a 15 orders of magnitude bigger)

$$= \frac{d_{\text{atom}}^3}{d_{\text{nuc}}^3}$$

$$= \frac{(10^{-10})^3}{(10^{-15})^3}$$

$$= \left(\frac{10^{-10}}{10^{-15}}\right)^3$$

$$= (10^5)^3$$

$$= 10^{15}$$

Example

How many orders of magnitude is the length of a metre stick longer than the width of a pencil?

$$\frac{1\text{m}}{0.01\text{m}} = 100 = 10^2$$

$$\frac{10^0}{10^{-2}} = 10^2$$

2 orders of magnitude longer